

ENCS4320, Applied Cryptography

Midterm Exam

Faculty of Engineering and Technology Electrical and Computer Engineering Department

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Name:	Answer	ID:

Q1) (10 points) True or False

- 1. The advantage of a stream cipher is that you can reuse keys.
 - a) True
 - b) False
- 2. The one-time-pad encryption scheme is CPA-secure.
 - a) True
 - b) False The one-time-pad is deterministic, so it can never be CPA-secure.
- **3.** Any private-key encryption scheme that is CPA-secure must also be computationally indistinguishable:
 - a) True
 - b) False
- **4.** If G' is a PRG, then $G(s) = G'(s) \oplus G'(\bar{s})$ is necessarily a PRG.
 - a) True
 - b) False

G is not necessarily a PRG. Suppose that *G'* is a PRG which outputs the first bit of the seed and applies another PRG *G''* to remainder: $G' = (b \parallel s'') = b \parallel G''(s'')$ where $b \in \{0,1\}, s'' \in \{\{0,1\}^{n-1}$. This *G'* is a PRG, but mow notice the first bit of G(s) is always 1, because $b \oplus \overline{b} = 1$ for any *b*.

- 5. If pseudorandom functions (PRF) exist, then pseudorandom generators (PRG) exist.
 - a) True
 - b) False

True, $G(k) := F_k(1) ||F_k(2)|| \cdots F_k(s)$ is a PRG (of stretch $n \cdot s$).

- **6.** Let *Enc*(*K*, *M*) be an IND-CPA secure encryption function. If Alice computes *Enc*("Hello", "World") and Bob computes *Enc*("Hello", "World"), they will always evaluate to the same ciphertext.
 - a) True
 - b) False

Because this encryption function is IND-CPA secure, the scheme cannot be deterministic; consequently, encrypting the same thing twice (even with the same key and value) must yield two unique ciphertexts.

- 7. The IV in counter (CTR) mode must be kept secret.
 - a) True
 - b) False
- **8.** CBC-mode encryption with PKCS#5 padding provides message integrity, as long as the receiver makes sure to verify the padding upon decryption.
 - c) True
 - d) False
- **9.** Any private-key encryption scheme that is CCA-secure must also be CPA-secure.
 - a) True
 - b) False
- **10.** Properly used, a MAC provides both confidentiality and integrity.
 - a) True
 - b) False

Q2) (10 points)

- 1- Which of the following are true about the Vigenere cipher?
 - a) The Vigenere cipher is computationally infeasible to break if the key has length 100, even if 1000s of characters of plaintext are encrypted.
 - b) The Vigenere cipher can always be broken, regardless of the length of the key and regardless of the length of plaintext being encrypted.
 - c) A Vigenere cipher with key of length 100 can be broken (in a reasonable amount of time) using exhaustive search of the key space.
 - d) The Vigenere cipher is perfectly secret if the length of the key is equal to the length of the messages in the message space.
- **2.** Let $G: \{0,1\}^s \to \{0,1\}^n$ be a secure PRG. Is $G'(k) = G(k) \bigoplus 1^n$ is secure PRG?
 - a) Yes it is secure
 - b) No it is not secure
 - c) It depends on the distinguisher algorithm *A*
 - d) Not enough information to determine
- 3- In the definition of perfect secrecy, what threat model is assumed?
 - a) The attacker can eavesdrop on as many ciphertexts as it likes
 - b) The attacker can eavesdrop on a single ciphertext
 - c) The attacker is able to interfere with the communication channel between the two honest parties.
 - d) The attacker can carry out a chosen-plaintext attack
- 4- Which of the following is NOT true about computational secrecy?
 - a) Computational secrecy currently relies on unproven assumptions
 - b) Computational secrecy means that it is trivial for an attacker to always learn the entire message
 - c) Computational secrecy only ensures secrecy against attackers running in some bounded amount of time
 - d) Computational secrecy allows an attacker to learn information about the message with small probability
- 5- Consider a pseudo one-time pad encryption scheme Π constructed using some function G. Which of the following did our proof of security for the pseudo one-time pad show?
 - a) Π is always perfectly secret, for any G
 - b) Π is always computationally secret, for any G
 - c) If G is a pseudorandom generator, then Π is perfectly secret
 - d) If G is a pseudorandom generator, then Π is computationally secret
- 6- Double-DES was broken with the following attack:
 - a) Linear cryptanalysis attack
 - b) Man-in-the-middle attack
 - c) Meet-in-the-middle attack
 - d) Start-from-the-middle attack

- **7-** Suppose Alice uses CBC Mode for encrypting a message *m*. However, she forgets the value she used for *IV*, but has *c* and *k*. Can she recover *m*?
 - a) Almost everything except m_1 (Where m_1 is the first block)
 - b) Can only recover m_{n-1}
 - c) Can only recover m_n
 - d) Almost everything expect m_1 and m_2
- 8- Say we use CBC-mode encryption based on a block cipher with 256-bit key length and 128-bit block length to encrypt a 512-bit message. How long is the resulting ciphertext?
 - a) 640 bits
 - b) 512 bits
 - c) 768 bits
 - d) Not enough information to determine.
- **9-** One type of attack **not** covered by the definition of secure MAC scheme.
 - a) Forgery attack
 - b) Collision Attack
 - c) Replay attack
 - d) Key recovery attack
- **10-** Which of the following is the most appropriate primitive for achieving message integrity between two users sharing a key?
 - a) Message authentication code
 - b) Block cipher
 - c) Collision-resistant hash function
 - d) Private-key encryption scheme

Q3) (5 points)

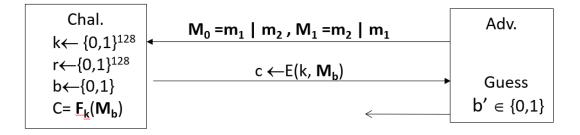
Let F be a block cipher with 128-bit block length. Consider the following encryption scheme for 256-bit messages: to encrypt message $M = m_1 \parallel m_2$ using key k (where $|m_1| = |m_2| = 128$, choose random 128-bit r and compute the ciphertext $r \parallel F_k(r) \oplus m_1 \parallel m_2$. Show how you could mount a valid chosen-plaintext attack (CPA) against this encryption scheme?

Let m_1 and m_2 be arbitrary but distinct. Using the encryption oracle, obtain an encryption $r||c_1||c_2$ of $m_1||m_2$. Output messages $M_0=m_1||m_2$ and $M_1=m_2||m_1$.

Not that the last block is not encrypted. Therefore,

if $c_2 = m_2 \rightarrow$ the challenge cipher for M_0 if $c_2 = m_1 \rightarrow$ the challenge cipher for M_1

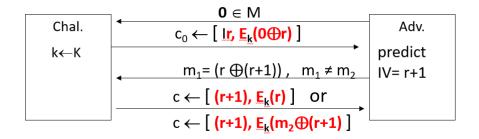
The attacker win the game with probability 1.



<u>Q4) (5 points)</u>

If Alice encrypts a message with AES-CBC, but instead of using completely random IVs, she uses r, r + 1, r + 2, and so on, where r is a random value that she chose once. Explain whither if this scheme is IND-CPA secure or not.

If the attacker can predict future IVs in AES-CBC, then AES-CBC is not IND-CPA secure.



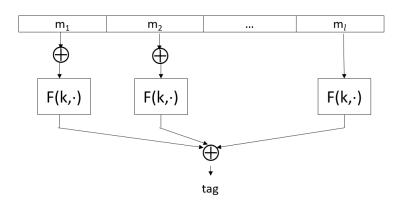
If $c = c_0$ them the challenge cipher for m_1 otherwise for m_2

<u>Q5) (5 points)</u>

Let *F* be a PRF. Show that the following constructions of MAC are insecure. Let $\mathcal{K} = \{0,1\}^n$ and $m = m_1 \parallel \dots \parallel m_\ell$ with $m_i \in \{0,1\}^n$ for $i \in [1, \ell]$.

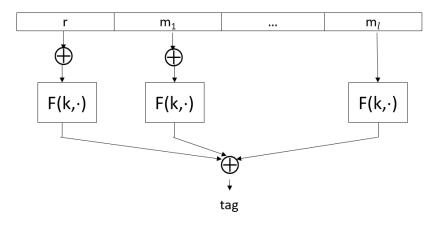
a) Send $t = F_k(m_1) \dots \oplus F_k(m_\ell)$.

If t is the tag for $m_1 ||m_2|| \cdots ||m_l$, t would be a valid forgery for $m_2 ||m_1||m_3|| \cdots ||m_l$ since changing the order of message blocks does not change the value of the tag given by $F_k(m_1) \bigoplus \cdots \bigoplus F_k(m_l)$.



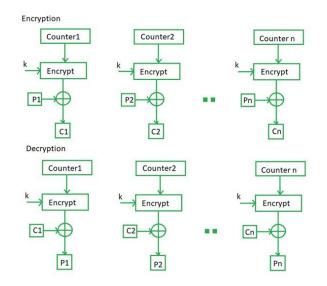
b) Pick $r \stackrel{U}{\leftarrow} \{0,1\}^n$, compute $t = F_k(r) \oplus F_k(m_1) \oplus ... \oplus F_k(m_\ell)$ and send (r, t).

A: Same attack (as in the previous part) works here. (r; t) remains a valid tag for any permutation of m_1, m_2, \ldots, m_l



Q6) (5 points)

Assume an honest user wants to send an 8-bit integer to their bank indicating how much money should be transferred to the bank account of an attacker. The user uses CTR-mode encryption based on a block cipher F with 8-bit block length. The attacker knows that the amount of money the user wants to transfer is exactly \$16, and has compromised a router between the user and the back. The attacker receives the ciphertext 10111100 01100001 (in binary) from the user. What ciphertext should the attacker forward to the bank to initiate a transfer of exactly \$32?



C (c₁c₀): 10111100 01100001

M(16): 0000000 00010000

Y: 10111100 01110001

M'(32) 0000000 00100000

C' 10111100 01010001

The answer may different depends on how you represent the data